

# 8. Sequences and Series

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8. (i) Find the value of

$$\sum_{r=4}^{\infty} 20 \times \left(\frac{1}{2}\right)^r$$

(3)

(ii) Show that

$$\sum_{n=1}^{48} \log_5 \left(\frac{n+2}{n+1}\right) = 2$$

(3)

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**Question 15 continued**

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9. Show that

$$\sum_{n=2}^{\infty} \left(\frac{3}{4}\right)^n \cos(180n)^\circ = \frac{9}{28}$$

(3)

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15. **In this question you must show all stages of your working.**  
**Solutions relying on calculator technology are not acceptable.**

Given that the first three terms of a geometric series are

$$12 \cos \theta \quad 5 + 2 \sin \theta \quad \text{and} \quad 6 \tan \theta$$

- (a) show that

$$4 \sin^2 \theta - 52 \sin \theta + 25 = 0 \quad (3)$$

Given that  $\theta$  is an obtuse angle measured in radians,

- (b) solve the equation in part (a) to find the exact value of  $\theta$  (2)

- (c) show that the sum to infinity of the series can be expressed in the form

$$k(1 - \sqrt{3})$$

where  $k$  is a constant to be found. (5)

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9. The first 3 terms of a geometric sequence are

$$3^{4k-5} \quad 9^{7-2k} \quad 3^{2(k-1)}$$

where  $k$  is a constant.

- (a) Using algebra and making your reasoning clear, prove that  $k = \frac{5}{2}$  (3)
- (b) Hence find the sum to infinity of the geometric sequence. (3)

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2. Jamie takes out an interest-free loan of £8100

Jamie makes a payment every month to pay back the loan.

Jamie repays £400 in month 1, £390 in month 2, £380 in month 3, and so on, so that the amounts repaid each month form an arithmetic sequence.

- (a) Show that Jamie repays £290 in month 12 (1)

After Jamie's  $N$ th payment, the loan is completely paid back.

- (b) Show that  $N^2 - 81N + 1620 = 0$  (2)

- (c) Hence find the value of  $N$ . (2)

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4. A sequence  $u_1, u_2, u_3, \dots$  is defined by

$$u_{n+1} = ku_n - 5$$

$$u_1 = 6$$

where  $k$  is a positive constant.

Given that  $u_3 = -1$

- (a) show that

$$6k^2 - 5k - 4 = 0 \tag{2}$$

- (b) Hence

(i) find the value of  $k$ ,

(ii) find the value of  $\sum_{r=1}^3 u_r$  (3)

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