

1. Constant Acceleration

Mr Faruk

Teacher of Mathematics
BSc/MSc/PGCE Mathematics

✉ cieigcsesolutions@gmail.com



SECTION B: MECHANICS

Answer ALL questions. Write your answers in the spaces provided.

Unless otherwise indicated, whenever a numerical value of g is required, take $g = 9.8 \text{ m s}^{-2}$ and give your answer to either 2 significant figures or 3 significant figures.

6.

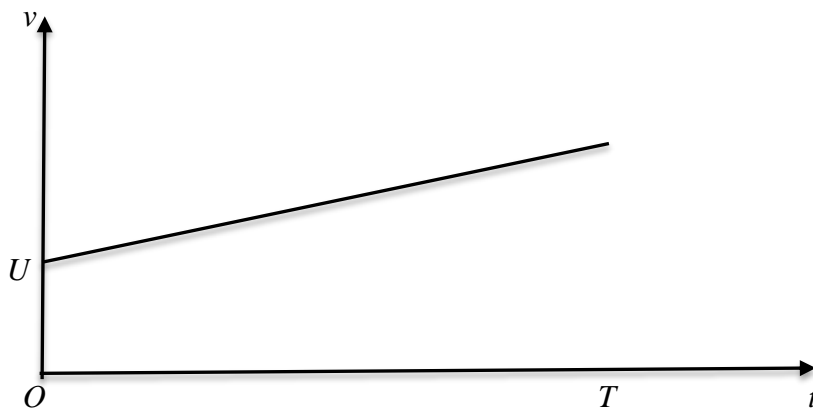


Figure 1

A car moves along a straight horizontal road. At time $t = 0$, the velocity of the car is $U \text{ m s}^{-1}$. The car then accelerates with constant acceleration $a \text{ m s}^{-2}$ for T seconds. The car travels a distance D metres during these T seconds.

Figure 1 shows the velocity-time graph for the motion of the car for $0 \leq t \leq T$.

Using the graph, show that $D = UT + \frac{1}{2} aT^2$.

(No credit will be given for answers which use any of the kinematics (*suvat*) formulae listed under Mechanics in the AS Mathematics section of the formulae booklet.)

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Question 1 continued

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(Total for Question 1 is 7 marks)

2. A train travels along a straight horizontal track from station P to station Q .

In a model of the motion of the train, at time $t = 0$ the train starts from rest at P , and moves with constant acceleration until it reaches its maximum speed of 25 m s^{-1}

The train then travels at this constant speed of 25 m s^{-1} before finally moving with constant deceleration until it comes to rest at Q .

The time spent decelerating is four times the time spent accelerating.

The journey from P to Q takes 700 s.

Using the model,

(a) sketch a speed-time graph for the motion of the train between the two stations P and Q . (1)

The distance between the two stations is 15 km.

Using the model,

(b) show that the time spent accelerating by the train is 40 s, (3)

(c) find the acceleration, in m s^{-2} , of the train, (1)

(d) find the speed of the train 572 s after leaving P . (2)

(e) State one limitation of the model which could affect your answers to parts (b) and (c). (1)

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1.

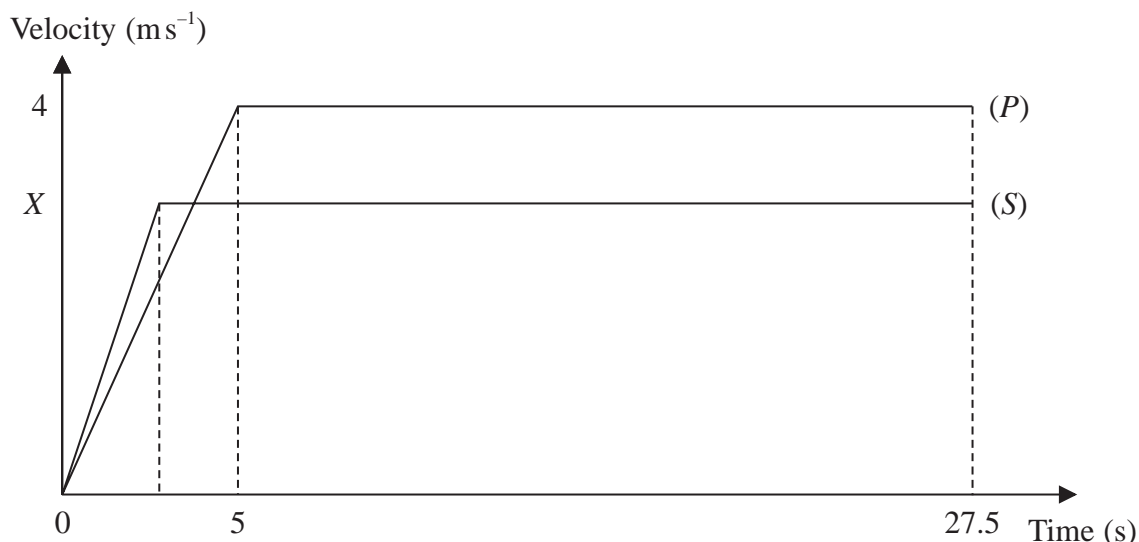


Figure 1

Two children, Pat (*P*) and Sam (*S*), run a race along a straight horizontal track.

Both children start from rest at the same time and cross the finish line at the same time.

In a model of the motion:

Pat accelerates at a constant rate from rest for 5 s until reaching a speed of 4 m s^{-1} and then maintains a constant speed of 4 m s^{-1} until crossing the finish line.

Sam accelerates at a constant rate of 1 m s^{-2} from rest until reaching a speed of $X \text{ m s}^{-1}$ and then maintains a constant speed of $X \text{ m s}^{-1}$ until crossing the finish line.

Both children take 27.5 s to complete the race.

The velocity-time graphs shown in Figure 1 describe the model of the motion of each child from the instant they start to the instant they cross the finish line together.

Using the model,

- (a) explain why the areas under the two graphs are equal, (1)
- (b) find the acceleration of Pat during the first 5 seconds, (1)
- (c) find, in metres, the length of the race, (2)
- (d) find the value of X , giving your answer to 3 significant figures. (4)

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Question 1 continued

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(Total for Question 1 is 3 marks)

2.

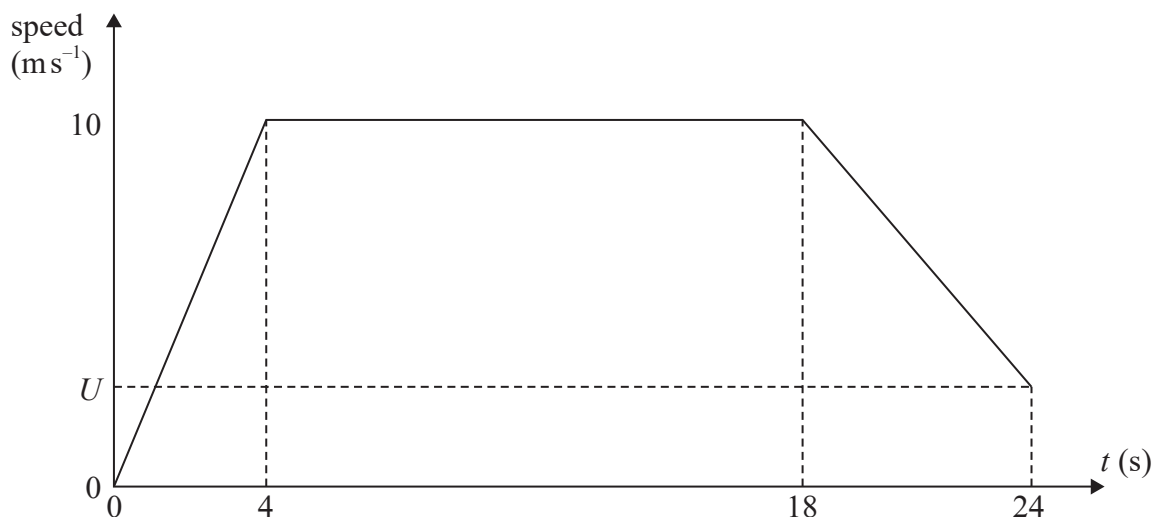


Figure 2

Figure 2 shows a speed-time graph for a model of the motion of an athlete running a **200 m** race in 24 s.

The athlete

- starts from rest at time $t = 0$ and accelerates at a constant rate, reaching a speed of 10 m s^{-1} at $t = 4$
- then moves at a constant speed of 10 m s^{-1} from $t = 4$ to $t = 18$
- then decelerates at a constant rate from $t = 18$ to $t = 24$, crossing the finishing line with speed $U \text{ m s}^{-1}$

Using the model,

- (a) find the acceleration of the athlete during the first 4 s of the race, stating the units of your answer, (2)
- (b) find the distance covered by the athlete during the first 18 s of the race, (3)
- (c) find the value of U . (3)

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